## Math, Music and Memory Fall 2014 Handout for Sections 2.2 and 2.3: Scales and Intervals

$\underline{\mathbf{Scale}}$	# of Notes		H-W Sequence					
Chromatic	12	All half steps						
Whone Tone	6		1	All w	hole	ste	ps	
Major	7	W	W	Н	W	W	W	Н
Natural Minor	7	W	Н	W	W	Н	W	W
Harmonic Minor	7	W	Н	W	W	Н	WH	Н

Figure 1: The five types of scales discussed in Section 2.2 and their defining sequences of half (H) and whole (W) steps.

## Examples

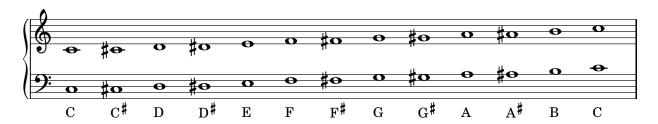


Figure 2: An ascending **chromatic scale** beginning on C. The scale has twelve notes, with consecutive notes always separated by a half step.



Figure 3: The two different whole tone scales, one beginning on C and the other on  $C^{\sharp}$ . In each case, the interval between consecutive notes is always equal to a whole step (two half steps).

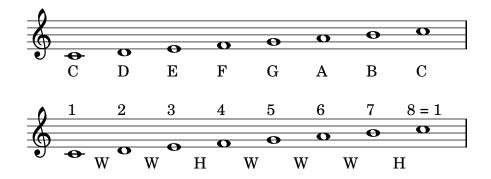


Figure 4: The **C** major scale. Notice the pattern of whole (W) and half (H) steps between consecutive notes. This same pattern holds for any major scale.

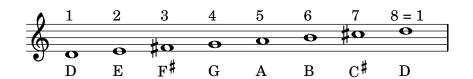


Figure 5: The **D** major scale in the treble clef.

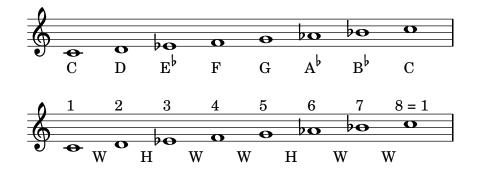


Figure 6: The **natural C minor scale**. Notice the pattern of whole (W) and half (H) steps between consecutive notes. This same pattern holds for any natural minor scale.

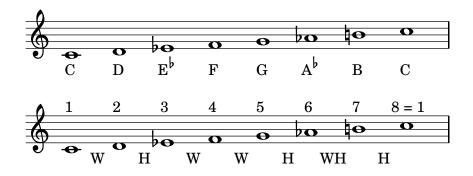


Figure 7: The **harmonic C minor scale**. The only difference from the natural C minor scale is that the seventh scale degree has been raised up a half step.

## **Intervals**

**Definition:** Two notes are an  $\underline{nth}$  interval apart if they are n steps from each other on the musical staff. When counting the number of steps, be sure to include the location of **both** the starting and ending note.

From a mathematical perspective, the definition of a musical interval is counter-intuitive because it over-counts the actual distance by one unit. The notes G and A are next to each other on the piano, so that should really be considered one step, not two. The notes A and C are two steps away on the piano keyboard, so that interval should really be a second, not a third. The musical version of measuring distance causes problems when combining intervals. For instance, we would expect that a second and a third combine to produce a fifth, but this is false! The interval from G to A (a second) plus the interval from A to C (a third) is equal to the interval from G to C (a fourth). According to music theory, the equation 2 + 3 = 4 is valid!

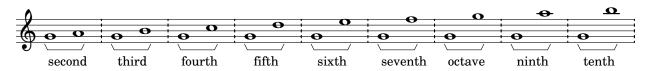


Figure 8: Some basic musical **intervals**. When counting the number of steps between two notes, always include the line or space of **both** the starting and ending note.

In addition to the number of steps in a musical interval, there is also the designation of **perfect**, **major** or **minor**, as well as augmented or diminished. The terms perfect and major are assigned to intervals corresponding to those found in the major scale. More specifically, if the major scale beginning on the bottom note contains the upper note as part of its scale, then the interval is perfect (in the case of the fourth or fifth) or it is major. The abbreviation for a major interval with n steps is Mn. Thus, M3 represents a major third and M6 means a major sixth. We use P4 and P5 to denote a perfect fourth and fifth, respectively.

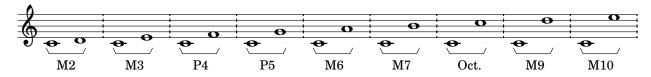


Figure 9: Some **major** (M) and **perfect** (P) intervals. In each case, the top note is a part of the C major scale.

If an interval is not perfect or major, we will consider it to be **minor**. The one exception is the interval that divides the octave in half, that is, an interval of six half steps, called a *tritone*. Some important minor intervals are shown in Figure 10, using middle C as the bottom note. Minor intervals are notated with a lower case m.

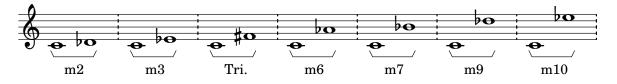


Figure 10: Some minor (m) intervals and the tritone (Tri.).

Scale Deg.	Interval	Half Steps	Name	Musical Example(s)	
1	Uni.	0	<u>Tonic</u>		
2	M2	2	Supertonic	Frère Jacques Happy Birthday to You	
3	М3	4	Mediant	Oh, When the Saints Kumbaya	
4	P4	5	Subdominant	Here Comes the Bride Oh Christmas Tree	
5	P5	7	Dominant	Twinkle Twinkle Little Star My Favorite Things	
6	M6	9	Submediant	My Bonnie Lies over the Ocean It Came upon a Midnight Clear	
7	M7	11	Leading tone	Take on Me	
8 = 1	Oct.	12	Octave	Somewhere over the Rainbow	

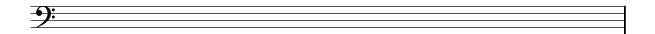
Table 1: The **major** (M) and **perfect** (P) intervals within the octave, including the number of half steps in each interval, and some sample musical examples.

Notes	Interval	Half Steps	Musical Example(s)
$C - D^{\flat}$	m2	1	Theme from Jaws
$\mathrm{C}-\mathrm{E}^{ abla}$	m3	3	"Air-ball!" (the heckle interval)  Greensleeves
$\mathrm{C}-\mathrm{F}^{\sharp}$	Tri.	6	Maria Theme from The Simpsons
$C - A^{\flat}$	m6	8	Theme from Love Story Go Down Moses
$C - B^{\flat}$	m7	10	There's a Place for Us

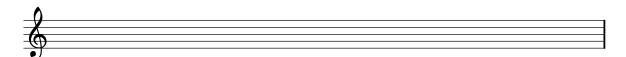
Table 2: The **tritone** (**Tri.**) and the **minor** (**m**) intervals within the octave, including the number of half steps in each interval, and some sample musical examples.

## Exercises (blank piano keyboard provided below for assistance)

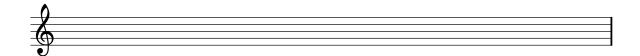
1. Write an ascending whole tone scale (one octave) using only flats in the bass clef beginning on G. Use whole notes and write the letter name below each note.



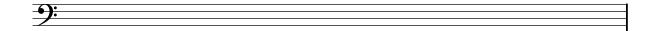
2. Write an ascending  $E^{\flat}$  major scale (one octave) in the treble clef. Use whole notes and write the letter name below each note.



3. Write an ascending  $C^{\sharp}$  natural minor scale (one octave) in the treble clef. Use whole notes and write the letter name below each note.



4. Write an ascending  $B^{\flat}$  harmonic minor scale (one octave) in the bass clef. Use whole notes and write the letter name below each note.



5. Notate each of the following musical intervals, including major, minor and perfect designations.



